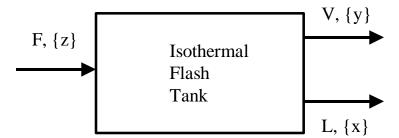
## Midterm Examination Number Three Administered: Friday-Monday, April 9-12, 1999

## Problem 1.

Consider an isothermal flash tank:



This unit takes a pressurized liquid, three-component feed stream and exposes it to a low pressure vessel maintained under isothermal conditions. The net result is that some of the fluid is vaporized, while some fluid remains liquid. The compositions of the liquid and vapor phase are determined by the combined analysis of mass balances and Raoult's Law for vapor-liquid equilibrium.

The temperature in the flash tank is T = 298K and the pressure in the tank is P = 101kPa.

Raoult's Law states that the product of the liquid mole fraction of component i and the vapor pressure of component i is equal to the partial pressure of component i in the vapor phase:

$$x_i P_i^{vap} = y_i P$$

Use the following vapor pressure data for the temperature given above

$$P_A^{vap} = 0.6bar @ T = 298K$$
  
 $P_B^{vap} = 1.0bar @ T = 298K$   
 $P_C^{vap} = 2.0bar @ T = 298K$ 

You know all the flowrates and the feed composition:

F = 100  mol/hr	V = 44.738 mol/hr	L = F - V mol/hr
$z_{A} = 0.4$	y <sub>A</sub> = ?	x <sub>A</sub> = ?
$z_{B} = 0.3$	y <sub>B</sub> = ?	x <sub>B</sub> = ?
$z_{\rm C} = 0.3$	y <sub>C</sub> = ?	x <sub>c</sub> = ?

Then you have six unknowns, the compositions of the liquid stream and the composition of the vapor stream. (a) Write equations which will yield the unknowns. Clearly identify the origin of each equation (mass balance, constraint, Raoult's Law)

(b) Convert these equations to a linear form with unknown terms on the left hand side and constants on the right hand side, if they are not already in that form.

(c) Convert the equations to matrices and vectors.

(d) Compute the determinant and rank of the matrix.

(e) Using MATLAB linear algebra functions, solve for the steady-state values of the unknown compositions. Show the MATLAB code.

(Hint: since you have 3 components, you will have three mass balances. You also have 2 streams with constraints that the sum of the mole fractions must be unity. You also have 3 Raoult's Law constraints Therefore, you have 8 equations. However, you only have 6 unknowns. Not all of the 8 equations are independent. You must choose 6 independent equations. Part (d) should indicate to you whether you have selected 6 independent equations.)

## Problem 2.

Consider the same flash tank describe in Problem (1). Now consider that the L and V stream flowrates are also unknowns. This makes the problem a set of 8 non-linear equations. Use systems or the MATLAB program of your choice to solve for liquid and vapor stream compositions and flow-rates. Use an initial guess of

<b>X</b> <sub>A</sub> =0.33	<b>X</b> <sub>B</sub> =0.33	<b>x<sub>C</sub></b> =0.33
y <sub>A</sub> =0.33	<b>y</b> <sub>B</sub> =0.33	y <sub>C</sub> =0.33
L=50  mol/hr	V=50 mol/hr	

Show your input file, syseqninput.m. Show your converged answer. Clearly indicate which variables are which.

## Problem 3.

In an isothermal batch reactor, the following reaction occurs:

 $A+2B \rightarrow C$ 

You know the initial concentrations of A, B, and C:  $A_0$ ,  $B_0$ , and  $C_0$ .

You record the concentration of C, C(t), as a function of time, t.

You repeat the experiment for several different temperatures, T. (Thus you have the concentration as a function of time and temperature.)

From kinetics, you know the rate of production of C is given by:

$$rate(t) = \frac{dC(t)}{dt} = A \cdot B^2 \cdot k_o \exp^{\frac{-Ea}{RT}} = (A_o - C) \cdot (B_o - 2C)^2 \cdot k_o \exp^{\frac{-Ea}{RT}}$$

You want to perform a regression to obtain the reaction rate constant,  $k_0$  and the activation energy,  $E_a$  but you couldn't measure the rate,  $\frac{dC(t)}{dt}$ , only the concentration C(t). (This is how the process usually works). To handle this, you can rearrange and analytically integrate this differential equation to yield:

$$k_{o} \exp^{\frac{-Ea}{RT}} t = \left(\frac{-2}{(B_{o} - 2A_{o})^{2}}\right) \left[ 2(B_{o} - 2A_{o})\left(\frac{1}{B_{o} - 2C} - \frac{1}{B_{o} - 2C_{o}}\right) - 2\ln\left(\frac{B_{o} - 2C}{B_{o} - 2C_{o}}\right) + \frac{1}{2}\ln\left(\frac{A_{o} - C}{A_{o} - C_{o}}\right) \right]$$

(a) Put this equation in a form like  $y = b_0 + b_1 x$  so that you could perform least squares linear regression on it to determine the reaction rate constant,  $k_0$  and the activation energy,  $E_a$ , from data which gives Clearly identify all four variables in this equation,  $y = b_0 + b_1 x$ . Clearly identify how to obtain  $k_0$  and  $E_a$  from the fit constants.

(b) Download the data file, xm03file.zip from the Homeworks section of the course website. This file has been zipped with WinZip. You must unzip the file using the WinZip utility, available on the computers in Dougherty 314. Once the file has been unzipped, you can read the data as an Excel spreadsheet (Excel 97, also available in Dougherty 314), which gives concentration as a function of time and temperature. From this data, calculate

(a)  $\mathbf{k}_{o}$  and  $\mathbf{E}_{a}$ 

(b) the standard deviations of  $k_0$  and  $E_a$ 

(c) the measure of fit of the model. Clearly indicate all answers. Do not simply provide an ambiguous program output.