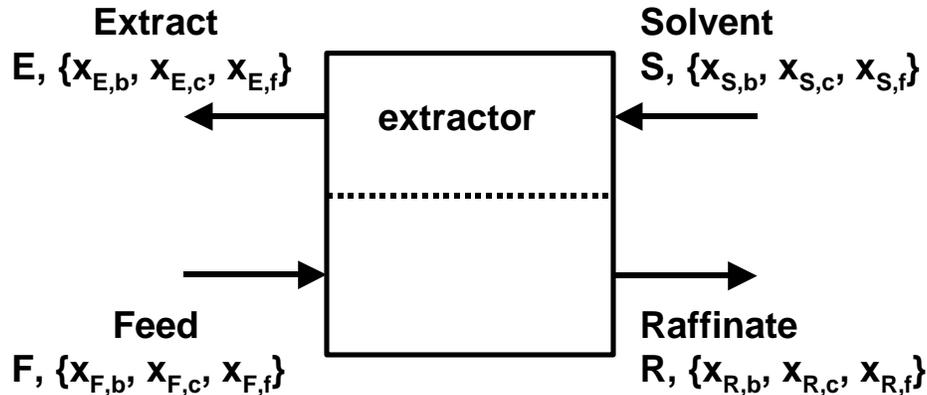


Applied Statistics and Numerical Methods for Engineers
ChE 301, Fall 1998
Midterm Exam Number Three
TAKE HOME EXAM
Assigned: Wednesday, November 11, 1998
Due: Friday, November 13, 1998, BEGINNING OF CLASS

THE EXAM HAS 48+54+20=122 POINTS.

Problem 1. (48 points)

Consider an extractor:



This unit uses a recycled furfural stream as the solvent to extract benzene from a cyclohexane product stream. The data you are given is

$F = F_0 \text{ mol/hr}$	$S = 150 \text{ mol/hr}$	$R = 95 \text{ mol/hr}$	$E = E_0 \text{ mol/hr}$
$x_{F,b} = 0.1$	$x_{S,b} = 0.0010$	$x_{R,b} = ?$	$x_{E,b} = ?$
$x_{F,c} = 0.9$	$x_{S,c} = 0.0001$	$x_{R,c} = ?$	$x_{E,c} = ?$
$x_{F,f} = 0.0$	$x_{S,f} = 0.9989$	$x_{R,f} = ?$	$x_{E,f} = ?$

You are to consider F_0 and E_0 as givens (not variables) defined by:

$$a = 100$$

$$b = 105$$

$$F_0 = \text{rand} \cdot (b - a) + a$$

$$E_0 = F_0 + S - R$$

where rand is the random number generator function of MATLAB.

The equilibrium constants are: $K_b = \frac{x_{E,b}}{x_{R,b}} = 20.0$ and $K_c = \frac{x_{E,c}}{x_{R,c}} = 0.05$.

Then you have six unknowns, the compositions of the raffinate stream and the composition of the extract stream.

- (a) Write equations which will yield the unknowns. Clearly identify the origin of each equation (mass balance, constraint, etc.) (12 points)
- (b) Convert these equations to a linear form with unknown terms on the left hand side and constants on the right hand side, if they are not already in that form. (12 points)
- (c) Convert the equations to matrices and vectors. (4 points)
- (d) Compute the determinant and rank of the matrix, and list the random values of F and E used in the calculation. (8 points)
- (e) Using MATLAB, solve for the steady-state values of the unknowns. (12 points)

(Hint: since you have 3 components, you will have three independent material balances. You also have 2 streams with constraints that the sum of the mole fractions must be unity. You also have 2 separation ratio constraints. Therefore, you have 7 equations. However, you only have 6 unknowns. Not all of the 7 equations are independent. You must choose 6 independent equations. Part (d) should indicate to you whether you have selected 6 independent equations.)

Problem 2. (54 points)

Use the data given in the file "file.xml3_pr2.dat" (available on the website) to determine if the data is best fit by a first, second, or third-order single-variable polynomial fit.

For the first order case, determine

- (a) the value of the model parameters (4 points)
- (b) the standard deviation of the model parameters (4 points)
- (c) the measure of fit of the model (2 points)
- (d) write out the model equation with the parameters you have obtained. (2 points)

For the second order case, determine

- (e) the value of the model parameters (6 points)
- (f) the standard deviation of the model parameters (6 points)
- (g) the measure of fit of the model (2 points)
- (h) write out the model equation with the parameters you have obtained. (2 points)

For the third order, determine

- (i) the value of the model parameters (8 points)
- (j) the standard deviation of the model parameters (8 points)
- (k) the measure of fit of the model (2 points)
- (l) write out the model equation with the parameters you have obtained. (2 points)
- (m) Based on this data determine which case is best. Justify. (4 points)

Problem 3. (20 points)

Consider the non-linear function:

$$f(x) = 0.001 \cdot \left[\left(\frac{x}{4} - 5 \right)^3 \sin \left(\frac{x}{4} + 4 \right) - \frac{x^2}{16} + 3 \right] \exp \left(\frac{-x}{40} \right)$$

- (a) How many roots are there between $x = 0$ and $x = 100$?
- (b) What are the roots of $f(x)$ between $x = 0$ and $x = 100$?
- (c) Plot the function over the range $x = 0$ to $x = 100$ with the line $y=0$ and circle the roots.