

Exam II

Administered: Tuesday, October 15, 2013

24 points

For each problem part:    0 points if not attempted or no work shown,  
                                     1 point for partial credit, if work is shown,  
                                     2 points for correct numerical value of solution

**Problem 1. (8 points)**

A particular device is powered by three batteries. Each battery has a mean life time of 10 months. The device only operates if all three batteries continue to function.

- (a) What PDF would describe the probability that an individual battery is operating after 6 months?
- (b) What is the probability that an individual battery is operating after 6 months?
- (c) What PDF would describe the probability that all 3 batteries are functioning after 6 months?
- (d) What is the probability that the device still operates after 6 months?

**Problem 2. (6 points)**

We run a warranty company that provides replacement parts for digital cameras. If our research team tells us that on average digital cameras have a lifetime of 4 years with a standard deviation of 1.5 years, then answer the following questions.

- (a) If we provide a warranty for all cameras lasting less than 1 years, what fraction of the cameras can we expect to replace?
- (b) If we only want to replace 1% of the cameras, how long should our warranty last?
- (c) What PDF did you use to solve (a) & (b)?

**Problem 3. (10 points)**

We are in charge of designing a secondary containment area for an area surrounding a series of large tanks containing concentrated sulfuric acid. The purpose of the containment area is to hold the sulfuric acid for a relatively short time in the event that one of the tanks springs a major leak. This containment area is to be concrete lined with a corrosion-resistant film. We are examining 2 types of films.

Film 1 is polycarbonate based. Studies of 12 experiments indicate that the average contact time before the film fails is 24 hours with a sample standard deviation of 2 hours.

Film 2 is a polymer/silica gel composite material. Studies of 16 experiments indicate that the average contact time before the film fails is 30 hours with a sample standard deviation of 4 hours.

A square foot of Film 2 is twice as expensive as a square foot of Film 1.

Based on this information, answer the following questions.

- (a) What PDF is appropriate for determining a confidence interval on the difference of means?
- (b) Find the lower limit on a 96% confidence interval on the difference of means.
- (c) Find the upper limit on a 96% confidence interval on the difference of means.
- (d) If our boss says that in order to justify the higher cost of Film 2, then we need to be 96% confident that Film 2 lasts at least 3 hours longer than Film 1, which film do we recommend? Why?
- (e) How confident are we that Film 2 lasts 3 hours longer than Film 1?