Exam I Administered: Monday, February 7, 2000 24 points

For each problem part:	0 points if not attempted or no work shown,
	1 point for partial credit, if work is shown,
	2 points for correct numerical value of solution

Problem 1. (10 points)

The plant manager in a fungicide manufacturing plant has been doing an internal study of quality control as a function of operator shift: He has found that, when the A-shift is at work from 6:00 AM to 2:00 PM, there is 99% of the product is Good. When the B-shift is at work from 2:00 PM to 10:00 PM, there is 97% of the product is Good. When the C-shift is at work from 10:00 PM to 6 A.M, there is 93% of the product is Good.

(a) Draw a Venn Diagram of the sample space for a random variable denoting the quality of the product.

- (b) What is the probability that the product is Good?
- (c) What is the probability that the product is Defective?
- (d) What is the probability that the product is Defective and C-shift was responsible?
- (e) Given that the product is Defective, what is the probability that the C-shift was responsible?

Problem 2. (4 points)

Consider two independent random variables x and y. The random variable y has mean $\mu_v = 8.00$ and

variance $\sigma_y^2=4.00$. The random variable x obeys the PDF

$$f(x) = \begin{cases} \left(\frac{e}{4e-4}\right)e^{-\frac{x}{4}} & \text{for } 0 < x < 4\\ 0 & \text{otherwise} \end{cases}$$

(a) What is the mean of
$$q(x) = e^{-\frac{3x}{4}}$$

(a) What is the mean of $g(x) = e^{-4}$ (b) What is the mean of h(x,y) = g(x) + 5y

Problem 3. (10 points)

Consider the joint PDF of two random variables, x and y,

$$f(x,y) = \begin{cases} \frac{4x}{3y} & \text{for } 0 < x < 1, y = 1,2 \\ 0 & \text{otherwise} \end{cases}$$

- (a) Is the random variable x continuous or discrete?
- (b) Is the random variable y continuous or discrete?
- (c) Show that this PDF is a legitimate PDF.
- (d) Find the probability, P(0 < x < 0.5, y = 1)
- (e) Find the probability , P(y = 2)